# Cognitively PL



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### Overview

- Types of constraints
- Explicit application of these constraints

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- Types of constraints
- Explicit application of these constraints
- Synergies from constraining several things at once







# Algorithmic Constrains Computational



- Hypothesis space: Established theory and modern modeling inform which hypothesis spaces are possible
  - Modeling has to explicitly define the hypothesis space and therefore make large assumptions about what universal assumptions children use in learning language

- Inference: Computational and Algorithmic diverge here
  - Computational takes the optimal inference given the problem & data



• Algorithmic takes the most "appropriate" inference based on our knowledge of humans

### Input/Output Constraints

• Input: Match as closely as possible with the input representation of the child

- Output: Instead of comparing against adult-level knowledge, compare the output against child-level trends.
  - Endgoal: Produce a representation of word segmentation in-line with children's representations based on background literature



## **Our Bayesian Strategy**

 $P(h|d) \propto P(d|h)P(h)$ 

- Ideal Learner-type model (Goldwater et al., 2009)
- Infer the simplest plausible lexicon
  - Smaller lexicon, shorter words in the lexicon
- Two implementations:
  - Unigram: No relationship between types of words that occur in sequence
  - Bigram: The preceding word informs which word is likely to follow

### Our Bayesian Strategy: Model #1

- Generative Rule:  $P(w_i|w_1, ..., w_{i-1}) = \frac{n_{i-1}(w_i) + \alpha P_0(w_i)}{i 1 + \alpha}$
- $n_{i-1}(w_i)$  is the number of times  $w_i$  occurs in the previous i-1 words
- α relates the likelihood of a novel word (and is free to vary, so we have to consider its prior, which is presumably concentrated around low values)
- P<sub>0</sub> is the specifications for the composition of a novel word how likely it is to be composed of certain phonemes or syllables
  - Enforces parsimony
  - Infers rules about the language (assuming  $P_0$  is free to vary, which was not 100% clear)

$$P_0 = P(w = x_1, \ldots, x_m) = \prod_j P(x_j)$$

# Our Bayesian Strategy: Model #2

$$P(w_i|w_{i-1} = w', w_1, \dots, w_{i-2}) = \frac{n_{i-1}(w', w_i) + \beta P_1(w_i)}{n_{i-2}(w') + \beta}$$

- $P_1$  is equivalent to the equation on the previous slide:  $P(w_i)$
- n<sub>i-1</sub>(w',w<sub>i</sub>) is the number of times the bigram w',w<sub>i</sub> occurs in the previous i words
- n<sub>i-2</sub>(w') is the number of times w' occurs
- β is a free parameter that controls how strong of a bias towards few bigrams the model has

### Input

- Infants use a mix of inputs:
  - Syllables (earliest use 2-3 months) for the model
  - Phonemes (earliest use ~9 months?)
  - Lexical Stress Patterns (earliest use ~8 months)
- Model Assumptions/Concessions:
  - Adult Syllabification & Maximum-Onset Principle vs ???
  - Phoneme-based model vs Phones
  - Syllabification occurs within words





# Output

- Useful Oversegmentations The "All," "Right," "Alright," "-ly," "-ing," lexicon
  - Lead to better segmentation elsewhere because they serve as markers you get the beginning and the end of two other words every time they appear
- Useful Undersegmentations The "couldi" "isthata" "lookatthekitty" lexicon
  Help produce syntactic rules
- In the end, we fudge things in the models favor as long as it fits a "useful" pattern
  - In this sense, the paper is very exploratory



### Inference

- Ideal "BatchOpt" (MCMC algorithm)
- Incremental Processing "OnlineOpt"
- Sub-optimal Decision Making "OnlineSubOpt" (Probability Matching)
- Recency Effect "OnlineMem" (Decayed MCMC)
  - Probability of sampling a boundary proportional to b<sub>a</sub><sup>-d</sup>
    - b<sub>a</sub> is the number of boundaries until the end of the current utterance
    - d is the decay rate



### **Model Evaluations**

$$Precision = \frac{\#correct}{\#guessed} = \frac{\#true \ positives}{\#true \ positives + \#false \ positives}$$
$$Recall = \frac{\#correct}{\#true} = \frac{\#true \ positives}{\#true \ positives + \#false \ negatives}$$
$$F-score = \frac{2 * Precision * Recall}{Precision + Recall}$$

- Word Tokens used as Unit (*the penguin eats the fish* = 5)
- Separate Training & Test Sets

### Model Evaluations

		Unigram		Bigram	
		Phoneme	Syllable	Phoneme	Syllable
Bayesian	BatchOpt	55.0 (1.5)	53.1 (1.3)	69.6 (1.6)	77.1 (1.4)
	OnlineOpt	52.6 (1.5)	58.8 (2.5)	63.2 (1.9)	75.1 (0.9)
	OnlineSubOpt	46.5 (1.5)	63.7 (2.8)	41.0 (1.3)	77.8 (1.5)
	OnlineMem	60.7 (1.2)	55.1 (0.3)	71.8 (1.6)	86.3 (1.2)
Other	Lignos 2012	7.0 (1.2)	87.0 (1.4)		
	TPminima	52.6 (1.0)	13.0 (0.4)		

• When compared to adults

### **Model Evaluations**

	Unigram			Bigram		
	Real	Morph	Func	Real	Morph	Func
BatchOpt	0.73	0.13	4.40	4.19	0.69	6.37
OnlineOpt	2.15	0.47	3.17	6.44	0.90	4.85
OnlineSubOpt	2.59	0.45	3.38	8.77	2.08	2.87
OnlineMem	2.19	0.31	5.02	14.41	3.20	3.64
Lignos 2012	19.00	3.59	0.03			
TPminima	0.01	0.00	7.33			0

- "Real" and "Morph" represent Oversegmentations
- "Func" represents Undersegmentations

### Modeling Human Performance - Frank et al., 2010

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number of types

• Facets of the data that ought to be more challenging for a human to "solve" word segmentation make it more difficult for Bayesian, but not other, models

